

1. Find the area of the region bounded by the line  $y = x$  and the parabola  $y = 6 - x^2$ .
2. Find the area of the region between  $x = 2 \cos x$  and  $x = 2 - 2 \cos x$ ,  $0 \leq x \leq \pi$
3. Find the area of the region between  $x = y^2$  and  $x = 32 - y^2$  from  $y = -2$  to  $y = 2$ .
4. Find the area of the region between lines  $x = -2y + 5$ ,  $x = y - 1$  and  $y = 0$ .
5. The base of a certain solid is the region in the  $xy$ -plane bounded by the parabolas  $y = x^2$  and  $x = y^2$ . Find the volume of this solid if every cross section perpendicular to the  $x$ -axis is a square with base in the  $xy$ -plane.
6. Find the volume of a pyramid with height  $h$  and rectangular base with dimensions  $b$  and  $2b$ .
7. Find the volume generated by rotating the region bounded by the given curves about the specified line.
  - (a)  $y = \frac{1}{x^4}$ ,  $x = \frac{1}{2}$ ,  $x = 1$ ,  $y = 0$ , about the  $y$ -axis
  - (b)  $y = x^3$ ,  $x = 0$ ,  $y = 27$ , about the  $x$ -axis
  - (c)  $y = \sqrt{x}$ ,  $y = 4x$ , about  $x = -1$
  - (d)  $y = x^2$ ,  $x = y^2$ , about  $y = 3$