Math 152/172

1. Find the area of the region bounded by the line y = x and the parabola $y = 6 - x^2$.

2. Find the area of the region between $x = 2\cos x$ and $x = 2 - 2\cos x$, $0 \le x \le \pi$

3. Find the area of the region between $x = y^2$ and $x = 32 - y^2$ from y = -2 to y = 2.

4. Find the area of the region between lines x = -2y + 5, x = y - 1 and y = 0.

5. The base of a certain solid is the region in the xy-plane bounded by the parabolas $y = x^2$ and $x = y^2$. Find the volume of this solid if every cross section perpendicular to the x-axis is a square with base in the xy-plane.

6. Find the volume of a pyramid with height h and rectangular base with dimensions b and 2b.

7. Find the volume generated by rotating the region bounded by the given curves about the specified line.

(a)
$$y = \frac{1}{x^4}, x = \frac{1}{2}, x = 1, y = 0$$
, about the *y*-axis

(b) $y = x^3, x = 0, y = 27$, about the *x*-axis

(c)
$$y = \sqrt{x}, y = 4x$$
, about $x = -1$

(d)
$$y = x^2, x = y^2$$
, about $y = 3$