

1. Find the integral

(a)  $\int (x^3 + 2x^2 - x)e^{3x} dx$

(b)  $\int \frac{\ln x}{x^2} dx$

(c)  $\int e^{3x} \sin(2x) dx$

2. Find the integral

(a)  $\int \sin^3 x \cos^4 x dx$

(b)  $\int_0^{\pi/8} \sin^2(2x) \cos^3(2x) dx$

(c)  $\int \sin^2 x \cos^4 x dx$

(d)  $\int_0^{\pi/4} \tan^4 x \sec^4 x dx$

(e)  $\int \tan^3 x \sec^3 x dx$

3. Write out the form of the partial fraction decomposition (do not try to solve)

$$\frac{20x^3 + 12x^2 + x}{(x^3 - x)(x^3 + 2x^2 - 3x)(x^2 + x + 1)(x^2 + 9)^2}$$

4. Evaluate the integral

(a)  $\int (4x^2 - 25)^{-3/2} dx$

(b)  $\int \frac{(x-1)^2}{5\sqrt{24-x^2+2x}} dx$

(c)  $\int \frac{5x^2 + x + 12}{x^3 + 4x} dx$

5. Use (a) the Midpoint Rule and (b) the Trapezoidal Rule to approximate the integral

$$\int_1^3 x^2 dx$$

with  $n = 4$ .

6. Determine whether the given integral is convergent or divergent.

(a)  $\int_1^{\infty} \frac{4 + \cos^4 x}{x} dx$

(b)  $\int_1^{\infty} \frac{3 + \sin x}{x^2} dx$

$$(c) \int_0^{\infty} \frac{1}{\sqrt{x} + e^{4x}} dx$$

7. Compute the following integrals or show that they diverge.

$$(a) \int_e^{\infty} \frac{dx}{x \ln^5 x}$$

$$(b) \int_{-\infty}^0 (1+x)e^x dx$$

$$(c) \int_{-\infty}^{\infty} \frac{6x^5}{(x^6+3)^3} dx$$

$$(d) \int_0^{2019} \frac{1}{\sqrt{2019-x}} dx$$