## Math 251. WEEK in REVIEW 5. Fall 2013

- 1. Given  $\vec{a} = <1, 1, 2 > \text{and } \vec{b} = <2, -1, 0 >$ . Find the area of the parallelogram with adjacent sides  $\vec{a}$  and  $\vec{b}$ .
- 2. Find an equation of the line through the point (1, 2, -1) and perpendicular to the plane

$$2x + y + z = 2$$

3. Find the distance from the point (1, -1, 2) to the plane

$$x + 3y + z = 7$$

- 4. Find an equation of the plane that passes through the point (-1, -3, 1) and contains the line x = -1 2t, y = 4t, z = 2 + t.
- 5. Find parametric equations of the line of intersection of the planes z = x + y and 2x 5y z = 1.
- 6. Are the lines x = -1 + 4t, y = 3 + t, z = 1 and x = 13 8s, y = 1 2s, z = 2 parallel, skew or intersecting? If they intersect, find the point of intersection.
- 7. Identify and roughly sketch the following surfaces. Find traces in the planes x = k, y = k, z = k
  - (a)  $4x^2 + 9y^2 + 36z^2 = 36$
  - (b)  $y = x^2 + z^2$
  - (c)  $4z^2 x^2 y^2 = 1$
  - (d)  $x^2 + 2z^2 = 1$
- 8. Find

$$\lim_{t \to 1} \left( \sqrt{t+3}\vec{i} + \frac{t-1}{t^2 - 1}\vec{j} + \frac{\tan t}{t}\vec{k} \right)$$

- 9. Find the unit tangent vector  $\vec{T}(t)$  for the vector function  $\vec{r}(t) = \langle t, 2 \sin t, 3 \cos t \rangle$ .
- 10. Evaluate

$$\int_{1}^{4} \left( \sqrt{t}\vec{i} + te^{-t}\vec{j} + \frac{1}{t^2}\vec{k} \right) dt$$

- 11. Find the length of the curve given by the vector function  $\vec{r}(t) = \cos^3 t \ \vec{i} + \sin^3 t \ \vec{j} + \cos(2t) \ \vec{k}, 0 \le t \le \frac{\pi}{2}.$
- 12. Find the curvature of the curve  $\vec{r}(t) = \langle 2t^3, -3t^2, 6t \rangle$ .
- 13. Sketch the domain of the function

$$f(x,y) = \sqrt{x^2 + y^2 - 1} + \ln(4 - x^2 - y^2)$$

14. Find the level curves of the function  $z = x - y^2$ .

- 15. Find  $f_{xyz}$  if  $f(x, y, z) = e^{xyz}$ .
- 16. The dimensions of a closed rectangular box are 80 cm, 60 cm, and 50 cm with a possible error of 0.2 cm in each dimension. Use differential to estimate the maximum error in surface area of the box.
- 17. Find parametric equations of the normal line and an equation of the tangent plane to the surface

$$x^3 + y^3 + z^3 = 5xyz$$

at the point (2, 1, 1).

- 18. Given that  $w(x,y) = 2\ln(3x+5y) + x 2\tan^{-1}y$ , where  $x = s \cot t$ ,  $y = s + \sin^{-1}t$ . Find  $\frac{\partial w}{\partial t}$ .
- 19. Let  $f(x, y, z) = \ln(2x + 3y + 6z)$ . Find a unit vector in the direction in which f decreases most rapidly at the point P(-1, -1, 1) and find the derivative (rate of change) of f in this direction.
- 20. Find  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$  if

$$xe^y + yz + ze^x = 0$$

21. Find the local extrema/saddle points for

$$f(x,y) = 2x^2 + y^2 + 2xy + 2x + 2y$$

22. Find the absolute maximum and minimum values of the function  $f(x, y) = x^2 + 2xy + 3y^2$  over the set D, where D is the closed triangular region with vertices (-1, 1), (2, 1), and (-1, -2).