Math 251. WEEK in REVIEW 6. Fall 2013

1. Find the integral $\iint_R \frac{y\cos y}{x}\,dA$, where $R = \{(x,y)|\, 1 \le x \le e^4, 0 \le y \le \pi/2\}$.

2. Evaluate $\iint_D \frac{y}{\sqrt{1+x^2}}\,dA$ where D is the region in the first quadrant bounded by $x = y^2$, $x = 4$, $y = 0$.

3. Evaluate $\int\int_R y^2 \sin \frac{xy}{2} dA$ where R is the region bounded by $x = 0$, $y = \sqrt{\pi}$, $y = x$.

4. Evaluate $\int_0^2 \int_{y/2}^1 e^{x^2}\, dx\, dy$ by reversing the order of integration.

5. Evaluate $\displaystyle\int_0^1 \int_{2x^2}^2 x^3 \sin y^3 \, dy \, dx$.

6. Graph the region and change the order of integration.

a) $\displaystyle\int_0^1 \int_0^{x^3} f(x,y)dy\,dx + \int_1^2 \int_0^{2-x} f(x,y)dydx$

b) $\displaystyle\int_0^1 \int_0^{\sqrt{y}} f(x,y)dxdy + \int_1^{\sqrt{2}} \int_0^{\sqrt{2-y^2}} f(x,y)dxdy$

7. Let the region D be the parallelogram with the vertices $(0,0)$, $(1,2)$, $(5,4)$, and $(4,2)$. Write the double integral $\displaystyle\iint_D f(x,y)\,dA$ as a sum of iterated integrals (with the least number of terms).

8. Sketch the region bounded by $y^2 = 2x$ (or $x = \frac{y^2}{2}$), the line $x + y = 4$ and the x-axis, in the first quadrant. Find the area of the region using a double integral.

9. Describe the solid which volume is given by the integral $\int_0^2 \int_{y^2}^4 (x^2 + y^2)dx\,dy$ and find the volume.

10. Find the volume of the solid bounded by

$z = 1 + x + y,\ z = 0, x + y = 1, x = 0, y = 0.$