

MATH 251, Section _____
Thursday, Nov. 11, 2010

Quiz 12 (Sections 14.4, 14.5).
Dr. M. Vorobets

Due Tuesday, Nov. 16 at the beginning of class.

NAME (print): _____

No credit for unsupported answers will be given. Clearly indicate your final answer.

1. [3 pts.] Use Green's Theorem to evaluate $\oint_C (1 + \tan x)dx + (x^2 + e^y)dy$ where C is the positively oriented boundary of the region enclosed by the curves $y = \sqrt{x}$, $x = 1$, and $y = 0$.

2. [2 pts.] Find the divergence of the vector field $\vec{F} = e^{xyz}\vec{i} + \sin(x - y)\vec{j} - \frac{xy}{z}\vec{k}$.

[more problems on back]

3. [5 pts.] Show that $\vec{F}(x, y, z) = yz(2x + y)\vec{i} + xz(x + 2y)\vec{j} + xy(x + y)\vec{k}$ is conservative and use this fact to evaluate $\int_C \vec{F} \cdot d\vec{r}$ along the curve C given by $\vec{r}(t) = (1 + t)\vec{i} + (1 + 2t^2)\vec{j} + (1 + 3t^3)\vec{k}$, $0 \leq t \leq 1$.