

Course Information

Course Number: Math 300

Course Title: Foundations of Mathematics

 Section:
 970 (Honors)

 Time:
 MWF 12:00-12:50*

Location: Blocker 105

Credit Hours: 3

*Note: The lectures will be streamed during the designated class time but will not be recorded for viewing later. You must attend the lecture (either face-to-face or remotely via Zoom) during the designated class time in order to view the lecture.

Instructor Details

Instructor: Oksana Shatalov
Office: Blocker 360C

E-Mail: <u>shatalov@math.tamu.edu</u> (In all emails put "your name, Math 300, and the

subject of the message" in the subject line.)

Office Hours: Online TR 5pm-6pm and by appointment.

*Note: Zoom links for office hours will be available in eCampus.

Course Description

Foundations of mathematics including logic, set theory, functions, and number theory.

Course Prerequisites

Grade of C or better in MATH 148, MATH 152 or MATH 172, or equivalent.

Special Course Designation

This is a W (writing intensive) course, which means that close attention will be paid to students' ability to write mathematical statements and proofs mathematically and grammatically correctly. About one third of the grade will depend on the writing. Since this is a W course, no student can pass the course without a passing grade on the writing portion (see below).

Course Learning Outcomes

The purpose of the course is to provide students with important foundational skills that will prepare them to be successful in higher level courses. Upon successful completion of the course, students will:

- Be able to construct and organize their mathematical reasoning.
- Develop skills for reading and writing mathematical proofs.



- Recognize and identify frequently used types of proofs.
- Master several mathematical concepts from logic and set theory.
- Identify concrete situations where the newly learned techniques can be applied.
- Recognize and recall the main definitions and results explained in the course.
- · Develop quantitative and problem-solving skills.

Be expected to present simple proofs, definitions and statement of theorems.

Textbook

Mathematical Proofs: A Transition to Advanced Mathematics, 4 th edition by Chartrand, Polimeni, and Zhang. Pearson (2018).

Note: The instructor will be providing examples and recommendations concerning math writing.

The following little book (**not required**) is a good source for many such recommendations: <u>Donald E. Knuth, Tracy Larrabee, Mathematical Writing</u>, The Mathematical Association of America 1989. ISBN 978-0883850633.

Some other books of this kind:

- Norman E. Steenrod, Paul R. Halmos, et al, How to Write Mathematics, Amer. Math. Soc. 1973.
 ISBN-13: 978-0821800553. (A collection of articles by famous mathematicians concerning writing.)
- Nicholas J. Higham, Handbook of Writing for the Mathematical Sciences, SIAM 1998. ISBN-13: 978-0898714203
- <u>Steven Krantz, A Primer of Mathematical Writing: Being a Disquisition on Having Your Ideas</u> Recorded, Typeset, Published, Read & Appreciated
- And here is the timeless treasure: a tiny beautiful book on writing: <u>William Strunk Jr., E. B. White, The Elements of Style</u>, Longman 1999 (there are zillions of other editions). ISBN-10: 020530902X, ISBN-13: 978-0205309023

Resource Materials

To reduce the spread of Covid and to ensure a uniform testing environment for all students, all in-class individual assessments (quizzes and exams) will be done electronically in eCampus. The exams will be proctored online over Zoom. In order to do this, the following technical requirements are needed:

- * Appropriate hardware (laptop or desktop computer, a second device such as a mobile phone, high-speed internet connection)
- * Appropriate software (PDF reader, Zoom on phone and computer, the latest update on an internet browser-Chrome or Firefox are recommended)

Grading Policy

The course grading will be based on the tables below. At the end of the semester you
will receive the grade you earned, according to the scale given. Due to FERPA privacy
issues, I cannot discuss grades over email or phone. If you have a question about
your grade, please schedule a one-on-one Zoom meeting with me.



• Since this course is an official *Writing Course*, about 1/3 of the grade is based on your ability to communicate your ideas. The most obvious way in which the "1/3" will be manifested is through specific assignments and papers in which writing will play an integral part. However, writing communication skills will also be considered in the normal course of grading homework and exams.

• Grade Ingredients

	ACTIVITY	%	DUE DATES, POLICIES AND REMARKS	
1.	Exam 1	20	Date: September 30 (tentatively). The exam will be proctored through Zoom. During the exam, you will be required to set up a streaming video camera (cell phone or USB webcam) in such a way that the proctor will be able to view your workspace during the exam. The proctoring sessions may be recorded. In order to receive credit for this course, you must consent to be proctored in this manner.	
2.	Exam 2	25	Date: November 20 (tentatively). The exam will be proctored through Zoom. During the exam, you will be required to set up a streaming video camera (cell phone or USB webcam) in such a way that the proctor will be able to view your workspace during the exam. The proctoring sessions may be recorded. In order to receive credit for this course, you must consent to be proctored in this manner.	
3.	Homework	15	It will be assigned approximately once per week (usually due Friday). It must be turned in on time. For full credit on the homework, you must show all work and justify your answers. Emphasis will be placed on writing carefully and precisely. Other submission guidelines will be posted separately on eCampus.	
4.	Quiz	8	Approximately once per week (Usually the quiz will be posted on eCampus on Tuesday 5pm and it will be due Wednesday 11am) . The duration of each quiz will vary but does not exceed 15 minutes. Each quiz will cover material previously taught in class. Review notes before the quiz. One lowest quiz grade (except of the last one) will be dropped at the end of the semester.	
5.	Writing Assignments	12	A series of five <i>Writings Assignments</i> will be assigned during the semester with the following due dates: 08/31, 09/21, 10/12, 10/19, 11/09. The purpose of these assignments is to learn how to sketch out ideas in writing and organize them in a logical order.	
6.	Final Exam (Term Paper)	20	There will be no written final but instead Term Paper. The paper will be an expository paper on a mathematical topic, and will be at least 2000 words long (not including diagrams and references). Instructions and list of possible topics will be provided in eCampus.	

Grading Scale



Range	Grade
[90, 100]	А
[80, 90)	В
[70, 80)	С
[60, 70)	D
[0,60)	F

Note: Since this is a W course, no student can pass the course without a passing grade on the writing portion (see table below). Specifically, if you get less than 60% on the writing portion, you will get an F for the course no matter what your performance on the rest of the course material. If you get between 60% and 70% on the writing portion, you will get no better than D for the course. Otherwise your grade is as shown in the above table.

Writing Portion Ingredients					
Homework (only problems labeled by "*")	20%				
Writing Assignments	25%				
Term Paper	55%				

Late Work

Late work will NOT be accepted unless you have a University approved reason and contact me within two working days of the missed assignment.

Appeal Policy

Students have one week upon the return of a lab, quiz, project or exam to notify their instructor of any inaccuracies in their graded work. No changes will be made after this one-week period and the grade will stand. You must present the actual, original assignment or assessment to your instructor before any consideration is made. For homework, please consult your grader.

Attendance and Make-Up Policies

Attendance is essential to complete this course successfully.

- Excused Absences: University student rules concerning excused and unexcused absences, as well as makeups, can be found at http://student-rules.tamu.edu/rule07. In particular, make-up exams and quizzes or late homework, writing assignments will NOT be allowed unless a University approved reason is given to me in writing. Notification before the absence is required when possible. Otherwise (e.g. accident, or emergency), you must notify me within two business days of the missed exam, quiz, or assignment to arrange a makeup.
- For Fall 2020 only, students may use the Explanatory Statement for Absence from Class form in lieu of a medical confirmation. Students must submit the Explanatory Statement for Absence from Class within two business days after the last date of absence.



- Working with Friends: Working together on homework is fine and encouraged, but each of you must write up your own solutions in your own words, notation and/or symbols and write the names of your collaborators at the top left corner of your homework. Copying a solution from a source and referencing the source is still considered a violation of academic integrity because you are submitting work for a grade that is not your own work. It is NOT permissible to discuss any aspect of any quiz, test or examination until ALL students have completed the it. The penalties for violating this policy will range from an F on an assignment or test, to failing in the course.
- **Internet Problems:** If you experience Internet connection issues during class time, please contact me as soon as possible to make sure you have access to content or activities you missed.
- Makeup Exams will only be allowed due to excused absences and the makeup must be taken as soon as possible after the missed exam. You will need to schedule to make up your exam within 3 business days of the originally scheduled time to allow for grades to be returned in a timely manner. If you know ahead of time you will be absent during an exam, you must notify me in advance.

Tentative Course Schedule

	Topic	TEXTBOOK SECTIONS
1	Language and logic.	2.1-2.9
2	Quantified Statements, Negations. Trivial and Vacuous Proofs.	2.10-2.11, 3.1
3	Direct Proofs, Proof by Cases, Disproving Statements.	3.2, 3.4, 5.5
4	Indirect Proofs, Existence and Uniqueness Proofs. Proof Evaluations. Proofs Involving Divisibility of Integers.	3.3, 5.2-5.4, 4.1
5	Induction and Strong Induction. The language of sets.	Chapter 6, § 4.1
6	Subsets. Operations on sets, unions and intersections. Power set. Cartesian product.	1.1-1.3,1.6
7	Exam 1. Proofs involving sets.	4.4
8	Proofs involving sets (continued). Arbitrary unions and intersections. Functions: Definitions and basic properties.	1.4, 4.4, 10.1
9	Image of function. Composition of functions. Surjective functions and Injective functions.	10.2, 10.4
10	Bijective functions. Invertible functions.	10.3,10.5
11	Functions and sets .	10.1
12	Division Algorithm and the Well-Ordering Principle. Greatest common divisors and Euclidean Algorithm.	12.1-12.4
13	Relatively Prime Integers and Fundamental Theorem of Arithmetics. Partitions.	12.5-12.6 1.5
14	Equivalence relations and partitions. Exam 2	9.1-9.4
15	Congruences.	4.2, 9.5-9.6

Technology Support

As much of our learning experience relies on technology, many students can get overwhelmed when something goes wrong or things get overwhelming. If you're looking for



a curation of online learning resources, consider checking out https://keeplearning.tamu.edu/. If your need is specific to a course-related technology issue, consider seeking help from the 24/7 TAMU IT Help Desk.https://it.tamu.edu/help/.

Learning Support

- The University Writing Center (UWC) is a resource to help you develop and refine the communication skills vital to success in college and beyond. Currently, you can choose to work with a trained UWC peer consultant via web conference or email. You can schedule an appointment to discuss any kind of writing project. Their consultants can work with you at any stage of your process. To schedule an appointment or to view their handouts, videos, or interactive learning modules, visit https://writingcenter.tamu.edu/.
- Help sessions TBA

Zoom Etiquette

REMOTE CLASS ATTENDEES.

When joining class remotely via ZOOM, please join with your audio off. When you have a question during class you may

- (1)use the "CHAT to everyone" feature to type your question,
- (2) use the "raise your hand" feature and wait for me to call on you, or
- (3) unmute yourself, politely interrupt me, and I will pause and give you time to ask your question.

It is important to me that the students joining remotely are involved in the class discussion, but it is best if we do this in an organized way.

OFFICE HOUR ATTENDEES

When joining office hours via ZOOM, please join with your audio off. Everyone attending office hours will be joining one room, so if you would like to ask a question during office hours, please "raise your hand" and wait to be called on. If you need to speak to me privately, and have not made an individual appointment with me, please let me know through a private CHAT message and I will move you to a breakout room where we can talk one-on-one.

University Policies

Attendance Policy

The university views class attendance and participation as an individual student responsibility. Students are expected to attend class and to complete all assignments.

Please refer to <u>Student Rule 7</u> in its entirety for information about excused absences, including definitions, and related documentation and timelines.



Makeup Work Policy

Students will be excused from attending class on the day of a graded activity or when attendance contributes to a student's grade, for the reasons stated in Student Rule 7, or other reason deemed appropriate by the instructor.

Please refer to <u>Student Rule 7</u> in its entirety for information about makeup work, including definitions, and related documentation and timelines.

Absences related to Title IX of the Education Amendments of 1972 may necessitate a period of more than 30 days for make-up work, and the timeframe for make-up work should be agreed upon by the student and instructor" (Student Rule 7, Section 7.4.1).

"The instructor is under no obligation to provide an opportunity for the student to make up work missed because of an unexcused absence" (<u>Student Rule 7, Section 7.4.2</u>).

Students who request an excused absence are expected to uphold the Aggie Honor Code and Student Conduct Code. (See <u>Student Rule 24</u>.)

Academic Integrity Statement and Policy

"An Aggie does not lie, cheat or steal, or tolerate those who do."

"Texas A&M University students are responsible for authenticating all work submitted to an instructor. If asked, students must be able to produce proof that the item submitted is indeed the work of that student. Students must keep appropriate records at all times. The inability to authenticate one's work, should the instructor request it, may be sufficient grounds to initiate an academic misconduct case" (Section 20.1.2.3, Student Rule 20).

You can learn more about the Aggie Honor System Office Rules and Procedures, academic integrity, and your rights and responsibilities at aggiehonor.tamu.edu.

Americans with Disabilities Act (ADA) Policy

Texas A&M University is committed to providing equitable access to learning opportunities for all students. If you experience barriers to your education due to a disability or think you may have a disability, please contact Disability Resources in the Student Services Building or at (979) 845-1637 or visit <u>disability.tamu.edu</u>. Disabilities may include, but are not limited to attentional, learning, mental health, sensory, physical, or chronic health conditions. All students are encouraged to discuss their disability related needs with Disability Resources and their instructors as soon as possible.



Title IX and Statement on Limits to Confidentiality

Texas A&M University is committed to fostering a learning environment that is safe and productive for all. University policies and federal and state laws prohibit gender-based discrimination and sexual harassment, including sexual assault, sexual exploitation, domestic violence, dating violence, and stalking.

With the exception of some medical and mental health providers, all university employees (including full and part-time faculty, staff, paid graduate assistants, student workers, etc.) are Mandatory Reporters and must report to the Title IX Office if the employee experiences, observes, or becomes aware of an incident that meets the following conditions (see <u>University Rule 08.01.01.M1</u>):

- The incident is reasonably believed to be discrimination or harassment.
- The incident is alleged to have been committed by or against a person who, at the time of the incident, was (1) a student enrolled at the University or (2) an employee of the University.

Mandatory Reporters must file a report regardless of how the information comes to their attention – including but not limited to face-to-face conversations, a written class assignment or paper, class discussion, email, text, or social media post. Although Mandatory Reporters must file a report, in most instances, you will be able to control how the report is handled, including whether or not to pursue a formal investigation. The University's goal is to make sure you are aware of the range of options available to you and to ensure access to the resources you need.

Students wishing to discuss concerns in a confidential setting are encouraged to make an appointment with <u>Counseling and Psychological Services</u> (CAPS).

Students can learn more about filing a report, accessing supportive resources, and navigating the Title IX investigation and resolution process on the University's <u>Title IX webpage</u>.

Statement on Mental Health and Wellness

Texas A&M University recognizes that mental health and wellness are critical factors that influence a student's academic success and overall wellbeing. Students are encouraged to engage in proper self-care by utilizing the resources and services available from Counseling & Psychological Services (CAPS). Students who need someone to talk to can call the TAMU Helpline (979-845-2700) from 4:00 p.m. to 8:00 a.m. weekdays and 24 hours on weekends. 24-hour emergency help is also available through the National Suicide Prevention Hotline (800-273-8255) or at suicidepreventionlifeline.org.

COVID-19 Temporary Amendment

Campus Safety Measures

To promote public safety and protect students, faculty, and staff during the coronavirus pandemic, Texas A&M University has adopted policies and practices for the Fall 2020 academic term to limit virus



transmission. Students must observe the following practices while participating in face-to-face courses and course-related activities (office hours, help sessions, transitioning to and between classes, study spaces, academic services, etc.):

- Self-monitoring—Students should follow CDC recommendations for self-monitoring. Students who have a fever or exhibit symptoms of COVID-19 should participate in class remotely and should not participate in face-to-face instruction.
- Face Coverings—<u>Face coverings</u> (cloth face covering, surgical mask, etc.) must be properly worn in all non-private spaces including classrooms, teaching laboratories, common spaces such as lobbies and hallways, public study spaces, libraries, academic resource and support offices, and outdoor spaces where 6 feet of physical distancing is difficult to reliably maintain. Description of face coverings and additional guidance are provided in the <u>Face Covering policy</u> and <u>Frequently Asked Questions (FAQ)</u> available on the <u>Provost website</u>.
- Physical Distancing—Physical distancing must be maintained between students, instructors, and others in course and course-related activities.
- Classroom Ingress/Egress—Students must follow marked pathways for entering and exiting classrooms and other teaching spaces. Leave classrooms promptly after course activities have concluded. Do not congregate in hallways and maintain 6-foot physical distancing when waiting to enter classrooms and other instructional spaces.
- To attend a face-to-face class, students must wear a face covering (or a face shield if they have an exemption letter). If a student refuses to wear a face covering, the instructor should ask the student to leave and join the class remotely. If the student does not leave the class, the faculty member should report that student to the Student Conduct office for sanctions. Additionally, the faculty member may choose to teach that day's class remotely for all students.

Personal Illness and Quarantine

Students required to quarantine must participate in courses and course-related activities remotely and must not attend face-to-face course activities. Students should notify their instructors of the quarantine requirement. Students under quarantine are expected to participate in courses and complete graded work unless they have symptoms that are too severe to participate in course activities.

Students experiencing personal injury or Illness that is too severe for the student to attend class qualify for an excused absence (See <u>Student Rule 7</u>, <u>Section 7.2.2</u>.) To receive an excused absence, students must comply with the documentation and notification guidelines outlined in Student Rule 7. While Student Rule 7, Section 7.3.2.1, indicates a medical confirmation note from the student's medical provider is preferred, for Fall 2020 only, students may use the Explanatory Statement for Absence from Class form in lieu of a medical confirmation. Students must submit the Explanatory Statement for Absence from Class within two business days after the last date of absence.