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Math 220 – Homework 1

Due Thursday 09/08 at the beginning of class

PART A

Problems from the textbook:

- Section 1.1 # 1(b,c,f,h,i,k);
- Section 1.4 # 8,9,10.

PART B

- 1. State the negation for each of the following statements.
 - (a) $\sqrt{5}$ is a rational number.
 - (b) 0 is a negative number.
 - (c) The area of the circle is at most 5π .
 - (d) Two sides of a triangle have the same length.
 - (e) The point P on the plane lies outside of the circle C.
- 2. For the open sentence P(x): 3x-5>10 over the domain N, determine:
 - (a) the values of x for which P(x) is a true statement.
 - (b) the values of x for which P(x) is a false statement.
- 3. For the open sentence $P(x):(x^2-16)(x^4-16)(x^8+16)=0$ over the domain **R**, determine:
 - (a) the values of x for which P(x) is a true statement.
 - (b) the values of x for which P(x) is a false statement.
- 4. Prove that the statement $\neg((\neg Q \land (P \Rightarrow Q)) \Rightarrow (\neg P))$ is a tautology, a contradiction, or neither. You must state which of the three it is as well as give the proof.
- 5. In each of the following statements identify the hypothesis (assumption) and conclusion.
 - (a) If a is irrational, then 2a is irrational.
 - (b) a^3 is an even integer whenever a is an even integer.
- 6. Without changing their meanings, convert each of the following sentences into a sentence having the form "If P, then Q."
 - (a) A function is integrable provided the function is continuous.
 - (b) A function is rational if it is a polynomial.
 - (c) "You fail only if you stop writing." (Ray Bradbury)
- 7. Without changing their meanings, convert each of the following sentences into a sentence having the form "P if and only if Q."

If a function has a constant derivative, then it is linear, and conversely.

- 8. Consider the statements: $P: 2016 \in 7\mathbb{Z}$, and $Q: 2016 \notin \mathbb{E}$. State each of the following statements in words and indicate whether it is true or false.
 - (a) P; (b) Q; (c) $\neg P$; (d) $P \lor Q$; (e) $P \land Q$; (f) $P \Rightarrow Q$; (g) $\neg Q \Rightarrow P$; (e) $P \Leftrightarrow Q$.