Math 220 – Homework 2 (HNR)

Due Thursday 09/15 at the beginning of class

PART A

Problems from the textbook:

- Section 1.1 # 2(c,e,f,h); 3(c,e,f,h) 5(b,c,e,f); D1(a).
- Section 1.2 # 5(b,c,e); 13c; D4

PART B

- 1. Express the following statements in symbols. (**Do not use** "⇒")
 - (a) Every even integer can be expressed as the sum of two odd integers.
 - (b) The square of any real number is positive.
- 2. Given a quantified statement

$$\forall x \in \mathbb{Z}^+, (\exists y \in \mathbb{Z}^+ \ni xy \in \mathbb{E}). \tag{1}$$

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- (a) Express the given statement (1) in words.
- (b) Express the **negation** of the given statement (1) in symbols. (**Do NOT** use the symbol ∉.)
- (c) Express the **negation** of the given statement (1) in words.
- 3. Negate the following statements:
 - (a) There is a politician who is honest or trustworthy.
 - (b) The number p is prime or the number q is not prime.
- 4. Given a quantified statement

$$\forall x \in \mathbb{R}, \ \exists n \in \mathbb{Z} \ \ni \ (n \le x < n+1). \tag{2}$$

- (a) Express the statement (2) in words.
- (b) Express the **negation** of the statement (2) in symbols. (Do NOT use the symbol ∉.)
- 5. Consider the following statement:

"If x is a real positive number, then there is a real positive number ε such that $x < \varepsilon$ but $\frac{1}{\varepsilon} < x$."

- (a) Express the given statement in symbols. (**Do not use** "⇒")
- (b) Express the **negation** of the given statement in symbols in a useful form.
- (c) Express the **negation** of the given statement in words.
- 6. Consider the following definition:

A real-valued function f(x) is said to be decreasing on the closed interval [a,b], if for all $x_1, x_2 \in [a,b]$, if $x_1 < x_2$, then $f(x_1) > f(x_2)$.

- (a) Write the negation of this definition.
- (b) Give an example of a decreasing function on [-1, 1].
- (c) Give an example of a function that is not decreasing on [-1, 1].