## Math 220 - Homework 4

## Due Wednesday 02/17 at the beginning of class

## PART A

Problems from the textbook:

- Section 1.3 \# 1(b,c), 2(a,b,c), 4, 6
- Section 1.4 \# 17, $21^{1}$


## PART B

1. Disprove the following statements:
(a) For all positive integers $x, y, z, x^{y^{z}}=\left(x^{y}\right)^{z}$.
(b) If $n \in\{1,2,3,4,5\}$, then $3 \mid\left(2 n^{2}+1\right)$.
(c) There exist odd integers $a$ and $b$ such that $4 \mid\left(3 a^{2}+7 b^{2}\right)$. (Hint: Use proof by contradiction.)
2. Prove the statement ' If $n$ is an odd integer, then $7 n-5$ is odd.') by
(a) a direct proof;
(b) a proof by contrapositive;
(c) a proof by contradiction.
3. Let $x, y \in \mathbf{R}$. Proof that if $x y \neq 0$, then $x \neq 0$ by using more than one method of proof.
4. Use proof by contradiction to prove that if $a$ and $b$ are odd integers, then $4 X\left(a^{2}+b^{2}\right)$.
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[^0]:    ${ }^{1}$ Hint: use problem 20.

