Foundations of Mathematics Thursday 3 September 2020

- 1. Use the roster method to specify the elements in each of the following sets and then write a sentence in English describing the set.
 - (a) $\{x \in \mathbb{R} \mid x^2 2x 4 = 0\}.$
 - (b) $\{n \in \mathbb{Z} \mid n^2 < 27\}.$
 - (c) $\{n \in \mathbb{N} \mid n^2 < 27\}.$
 - (d) $\{x \in \mathbb{Q} \mid x^2 2x 4 = 0\}.$
- 2. Use set builder notation to specify the following sets.
 - (a) The set of all natural numbers with square at least 15.
 - (b) The set of all odd integers.
 - (c) The set of all real numbers at most 10 whose square exceeds 3.
 - (d) The set of positive rational numbers.
- 3. Write the following English sentences as mathematical statements involving quantifiers.
 - (a) A trangle has three sides.
 - (b) The square of a real number is nonnegative.
 - (c) Some Aggies are not Human.
 - (d) An integer is necessarily prime or composite.
 - (e) Some even numbers are divisible by two and are divisible by seven.
 - (f) The sum of two even integers is an odd integer.
 - (g) Irrational numbers are real.
- 4. Negate each of the quantified statements from Question 1.
- 5. Recall the following property of the integers: "If n is an integer, then there is an ingeger m with the property that n + m = 0."
 - (a) Write this as a statement involving quantifiers.
 - (b) Give a useful negation of this statement.
 - (c) What is this property called?