

Example

Aiden, Beverley, Charlie, and Danielle have inherited a house and a car to share equally. They each submit sealed bids for both items. Describe a fair division of these items using the Knaster Inheritance procedure (tell who gets each item and how much money each person gets or pays).

	House	Car
Step 1	Aiden bid \$120,000	Aiden bid \$8,000
	Beverley bid \$140,000	Beverley bid \$7,000
	Charlie bid \$150,000	Charlie bid \$6,500
	Danielle bid \$115,000	Danielle bid \$8,500
Step 2	_____ gets the house and _____	_____ gets the car and _____
	places _____	places _____
	in a holding account.	in a holding account.

Holding
Acct:

Steps 3-4	Aiden	Aiden
	Beverley	Beverley
	Charlie	Charlie
	Danielle	Danielle

Step 5	Aiden
	Beverley
	Charlie
	Danielle

Example

Four people were bidding for tickets to concert. Owen bid \$400, Madeline bid \$350, Sofia bid \$420, and Samuel bid \$380.

- (a) Who wins the tickets?
- (b) How much does he/she pay for the tickets?

Example

People are bidding on a vacation package on eBay. The minimum bid was set at \$500, and the bid increment is \$8. Complete the following chart to show the progress of the auction before time ran out.

(a)

Bidder	Bid	Current Winner	Current eBay bid
Lily	\$800	Lily	\$500
Nora	\$600		
Devin	\$650		
Nora	\$750		
Samuel	\$850		
Lily	\$1500		
Samuel	\$950		

- (b) Who won the auction?
- (c) How much did he/she pay for the vacation package?

Example

A county has 11 representatives to apportion to the towns listed below.

(a) Apportion the representatives using the Hamilton method.

Town	Pop.	
A	1500	
B	2200	
C	1640	
D	50	

(b) Apportion the representatives using the Jefferson method.

Town	Pop.	q	
A	1500	3.061	
B	2200	4.490	
C	1640	3.347	
D	50	0.102	

$d =$

(c) Apportion the representatives using the Webster method.

Town	Pop.	q	
A	1500	3.061	
B	2200	4.490	
C	1640	3.347	
D	50	0.102	

$d =$

(d) Apportion the representatives using the Hill-Huntington method.

Town	Pop.	q	
A	1500	3.061	
B	2200	4.490	
C	1640	3.347	
D	50	0.102	

$d =$

The Jefferson method favors large states. The Hill-Huntington method favors small states.

Example

Label each situation with one of the following five choices:

- A. The Alabama paradox occurred.
- B. The population paradox occurred.
- C. The new states paradox occurred.
- D. The quota condition was violated.
- E. The quota condition was NOT violated, and no paradox occurred.

- (a) A new state was added (along with a proportionate number of representatives) and yielded the following apportionments using the Hamilton method.

State	Original Apportionment	New Apportionment
G	8	8
H	5	5
I	3	3
J		2

- (b) The seats were apportioned using the Jefferson method.

State	quota	Jeff. App.
G	124.05	124
H	43.27	43
I	5.94	6

- (c) A new state was added (along with a proportionate number of representatives) and yielded the following apportionments using the Hamilton method.

State	Original Apportionment	New Apportionment
G	8	7
H	5	6
I	3	3
J		2

- (d) The house size changed from 8 to 9 and yielded the following apportionments using the Hamilton method.

State	House Size 8	House Size 9
G	5	4
H	3	4
I	0	1

- (e) As the population changes, the representation is reapportioned using the Hamilton method.

State	Original Apportionment	New Apportionment	Absolute Pop Change	Relative Pop Change
G	14	14	1000	1.1%
H	13	14	1200	3%
I	16	15	1400	2%

- (f) As the population changes, the representation is reapportioned using the Hamilton method.

State	Original Apportionment	New Apportionment	Absolute Pop Change	Relative Pop Change
G	14	14	1000	1.1%
H	13	14	1200	1.5%
I	16	15	1400	2%

- (g) The seats were apportioned using the Jefferson method.

State	quota	Jeff. App.
G	124.95	126
H	43.27	43
I	5.34	5